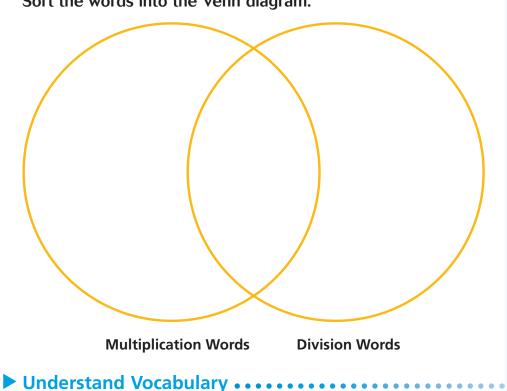


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Online

Vocabulary Builder



Review Words

Distributive Property divide dividend division divisor factor multiplication product quotient **Preview Words** compatible numbers multiple partial quotient remainder

Write the word that answers the riddle.

- I am the method of dividing in which multiples of the divisor are subtracted from the dividend and then the quotients are added together.
- 2. I am the number that is to be divided in a division problem.
- 3. I am the amount left over when a number cannot be

divided equally.

4. I am the number that divided the dividend.

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Name _____

Estimate Quotients Using Multiples

Essential Question How can you use multiples to estimate quotients?

UNLOCK the Problem REAL WORLD

The bakery made 110 pumpkin muffins. They will be packed in boxes with 8 muffins in each box. About how many boxes will there be?

You can use multiples to estimate.

A **multiple** of a number is the product of a number and a counting number. 1, 2, 3, 4, and so on, are counting numbers.



Think: What number multiplied by 8 is about 110?

STEP 1 List the multiples of 8 until you reach 110 or greater.

| Counting number | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
|--------------------|---|----|----|----|---|---|----|----|---|----|----|----|----|-----|
| Multiple of 8 | 8 | 16 | 24 | 32 | | | 56 | 64 | | | | 96 | | 112 |

STEP 2 Find the multiples of 8 that 110 is between.

13 × 8 = _____

14 × 8 =

110 is between _____ and _____, so $110 \div 8$ is between 13 and 14.

| 110 is closest to | , so $110 \div 8$ is about |
|-------------------|----------------------------|
| | |

So, there will be about _____ boxes.

Try This!

List the next 8 multiples of 10.

10, 20,

List the next 7 multiples of 100.

100, 200, _____



MATHEMATICAL PRACTICES

Chapter 4 137

Math Talk When estimating a quotient, how do you know which two numbers it is between? Explain.

| Example Estimate 196 ÷ 4 |
|---|
| Think: What number times 4 is about 196? |
| STEP 1 List the next 6 multiples of 4. |
| 4, 8, 12, 16, |
| Are any multiples close to 196? |
| Think: If I multiply by multiples of 10, the products will be greater. Using multiples of 10 will get me to 196 faster. |
| STEP 2 Multiply 4 by multiples of 10. |
| $10 \times 4 = 40$ |
| $20 \times 4 = 80$ |
| 30 × 4 = |
| 40 × 4 = |
| 50 × 4 = |
| The quotient is between 40 and 50. |
| $	imes$ 4 is closest to, so 196 \div 4 is about |

Share and Show

1. A restaurant has 68 chairs. There are six chairs at each table. About how many tables are in the restaurant?

Estimate. 68 ÷ 6

Think: What number times 6 is about 68?

- 10 × 6 =
- 11 × 6 =
- $12 \times 6 =$

68 is closest to _____, so the best estimate is

about ______ tables are in the restaurant.

Math Talk When do you multiply the divisor by multiples of 10 to estimate a quotient? Explain.

MATHEMATICAL PRACTICES

| 41 ÷ 3 | | | 2 ÷ 5 | |
|---------------------------------|----------------|----------|---------------|-------------------------|
| n Your Own d two numbers the | | | • • • • • • • | • • • • • • • • • • • • |
| timate the quotient 90 ÷ 7 | 5. 67 | ÷ 4 | 6. | 281 ÷ 9 |
| 102 ÷ 7 | 8. 85 | ÷ 6 | 9. | 220 ÷ 8 |
| 443 ÷ 5 | 11. 95 | ÷ 8 | 12. | 49 ÷ 3 |
| 249 ÷ 8 | 14. 412 | 2 ÷ 7 | 15. | 177 ÷ 9 |
| | | | | |

16. $83 \div 8$ 10
 17. $155 \div 4$ 40
 18. $70 \div 6$ 11

 19. $416 \div 5$ 80
 20. $194 \div 2$ 90
 21. $200 \div 3$ 70

Problem Solving REAL WORLD

22. The second se



- **23.** A mother bottlenose ate about 278 pounds of food in one week. About how much food did she eat in a day?
- 24. Write Math Four families went out for lunch. The total food bill came to \$167. The families also left a \$30 tip for the waitress. If each family spent the same amount, about how much did each family spend on dinner? Explain how you found your answer.

- **25.** What's the Question? A dolphin's heart beats 688 times in 6 minutes. Answer: about 100 times.
- **26. Test Prep** Small groups of about 7 bottlenose dolphins live together in pods. Sometimes several pods join in a herd to help protect each other. About how many pods are there in a herd of 204 dolphins?

(A) about 20 (C) about 40

B about 30 D about 1,400

SHOW YOUR WORK

Name ____

Remainders

Essential Question How can you use models to divide whole numbers that do not divide evenly?

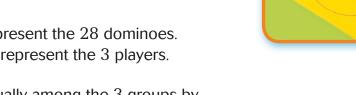
Investigate

Materials counters

Erica and 2 friends are playing a game of dominoes. There are 28 dominoes in the set. Erica wants each player to receive the same number of dominoes. Can she divide them equally among the 3 players? Why or why not?

You can use division to find the number of dominoes each player will receive.

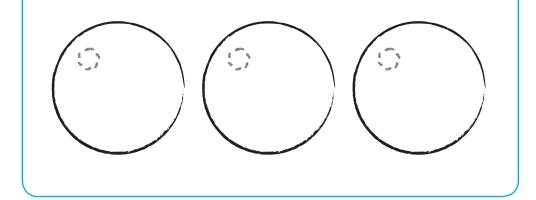
A. Use 28 counters to represent the 28 dominoes. Then draw 3 circles to represent the 3 players.





B. Share the counters equally among the 3 groups by placing them in the circles.

Draw a quick picture to show your work.



C. Find the number of counters in each group and the number of counters left over. Record your answer.

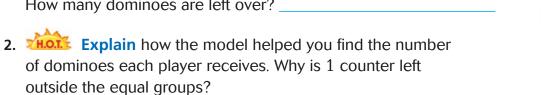
____ counters in each group

_ counter left over

Draw Conclusions

1. How many dominoes does each player receive?

How many dominoes are left over? _____



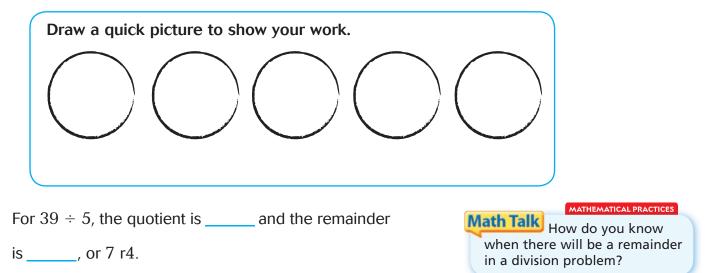
3. Apply Use counters to represent a set of 28 dominoes. How many players can play dominoes if each player receives 9 dominoes? Will any dominoes be left over? Explain.

Make Connections

When a number cannot be divided evenly, the amount left over is called the **remainder**.

Use counters to find $39 \div 5$.

- Use 39 counters.
- Share the counters equally among 5 groups. The number of counters left over is the remainder.



| | ne | | | | | |
|-----|-----------------|--|----------------|--------|-------------------|--------|
| Sh | are and s | Show MATH BOARD | • • • • • • | | •••• | |
| Use | e counters to f | ind the quotient and re | mainder. | | | |
| 1. | 10 ÷ 3 | 2. 28 ÷ 5 | 3. | 15 ÷ 6 | 4. | 11 ÷ 3 |
| 5. | 9)26 | 6. 22 ÷ 3 | 7. | 4)19 | 8. | 4)38 |
| 9. | 29 ÷ 4 | 10. 34 ÷ 5 | 11. | 25 ÷ 3 | _ ∛ 12. | 7)20 |
| | | ick picture to help. | | | - | |
| 13. | 19 ÷ 3 | | 14. | 5)47 | | |
| | | | | | | |
| | | | | | | |
| 15. | 4)35 | | ৰ্থ 16. | 23 ÷ 8 | | |
| | | | | | | |
| | | | | | | |
| | | | | | | |
| 17. | | Explain how you use a stient and remainder. | ı quick pic | ture | | |
| | | | | | | |
| | | | | | | |
| | | | | | | |

Problem Solving REAL WORLD

18. Macy, Kayley, Maddie, and Rachel collected 13 marbles. They want to share the marbles equally. How many marbles will each of the 4 girls get? How many marbles will be left over?

Frank used a model to solve this problem. He says his model represents $4\overline{)13}$. What is his error?



Look at the way Frank solved this problem. Find and describe his error.

Draw a correct model and solve the problem.

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| | So, eac |
| | marble |
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| | |

o, each of the 4 girls will get _____ arbles and _____ marble will be ft over.

Interpret the Remainder

Essential Question How can you use remainders in division problems?

UNLOCK the Problem REAL WORLD

Magda has some leftover wallpaper 73 inches long. She wants to cut it into 8 pieces to use around the photos in her scrapbook. Each piece will have equal length. How long will each piece be? When you solve a division problem with a remainder, the way you interpret the remainder depends on the situation and the question. **One Way** Write the remainder as a fraction. The divisor is _____ pieces. The is 73 inches. 9 r1 Divide to find the quotient and remainder. 8)73 Remember You can use multiples, The remainder represents 1 inch left over, which can also be divided into 8 equal parts and written as a fraction.

> remainder _ divisor

Write the quotient with the remainder written as a fraction.

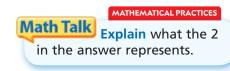
So, each piece will be _____ inches long.

Try This!

Jim made 32 ounces of soup for 5 people. How many ounces will each person get? Complete the division.



Each person gets _____ ounces.



counters, or draw a quick picture to divide.

Chapter 4 145

🚺 Other Ways

Output A set of the set of the

Ben is a tour guide at a glass-blowing studio. He can take no more than 7 people at a time on a tour. If 80 people want to see the glass-blowing demonstration, how many groups of 7 people will Ben show around?

First, divide to find the quotient and remainder. Then, decide how to use the quotient and remainder.

The quotient is _____.

11 r $7\overline{)80}$

The remainder is _____.

Ben can give tours to 7 people at a time. The quotient is the number of tour groups of exactly 7 people he can show around.

So, Ben gives tours to _____ groups of 7 people.

B Add 1 to the quotient.

If Ben gives tours to all 80 people, how many tours will he give? A tour can have no more than 7 people. To show all 80 people around, Ben will have to give 1 more tour.

So, Ben will give tours in all for 80 people.

G Use only the remainder.

Ben gives tours to all 80 people. After he completes the tours for groups of 7 people, how many people are in his last tour?

The remainder is 3.

So, Ben's last tour will have _____ people.

Try This!

Students are driven to soccer games in vans. Each van holds 9 students. How many vans are needed for 31 students?

Divide. $31 \div 9$

Since there are students left over, vans are needed to carry 31 students.

MATHEMATICAL PRACTICES

Math Talk Explain why you would not write the remainder as a fraction when you find the number of vans needed.



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Name .

Share and Show MATH

- Olivia baked 53 mini-loaves of banana bread to be sliced for snacks at a craft fair. She will place an equal number of loaves in 6 different locations. How many loaves will be at each location?
 - **a.** Divide to find the quotient and remainder.
 - **b.** Decide how to use the quotient and remainder to answer the question.

Interpret the remainder to solve.

- What if Olivia wants to put only whole loaves at each location? How many loaves will be at each location?
- S. Ed carves 22 small wooden animals to sell at the craft fair. He displays them in rows with 4 animals in a row. How many animals will not be in equal rows?

6)53

On Your Own

Interpret the remainder to solve.

- 4. Myra has a 17-foot roll of crepe paper to make 8 streamers to decorate for a party. How long will each streamer be if she cuts the roll into equal pieces?
- 5. Juan has a piano recital next month. Last week he practiced for 15 hours in all. Each practice session is 2 hours long. How many full practice sessions does Juan complete?
- 6. A total of 25 students sign up to be hosts on Parent's Night. Teams of 3 students greet parents. How many students cannot be on a team? Explain.

Problem Solving REAL WORLD

Use the picture for 7–9.

- **7.** Cho is making sock puppets just like the one in the picture. If she has 53 buttons, how many puppets can she make?
- Pose a Problem Write a question about Cho and the sock puppets for which the answer is 3.
 Explain the answer.



9. (Write Math >> How many more buttons will Cho need if she wants to make 12 puppets? Explain.

- **10.** Jonah cuts a board that is 33 inches long into 4 pieces of equal length. He uses the pieces for the sides of a picture frame. He puts an extra 2-inch wide trim on each side of the frame. How wide is the final frame?
- **11. Test Prep** Mr. Alia gives a "Good Job" badge to each of the 74 students who help at a school event. There are 8 badges in a package. How many packages will he open?



Name _

Divide Tens, Hundreds, and Thousands

Essential Question How can you divide numbers through thousands by whole numbers through 10?

UNLOCK the Problem REAL

Dustin is packing apples in gift boxes. Each gift box holds 4 apples. How many boxes can Dustin pack with 120 apples?

You can divide using basic facts and place value. Example 1 Divide. 120 ÷ 4 **STEP 1** Identify the basic fact. 12 ÷ 4 120 = _____ tens **STEP 2** Use place value. 12 tens \div 4 = tens \leftarrow Think: 4 \times 3 tens = 12 tens **STEP 3** Divide. = ____ $120 \div 4 = 30$ So, Dustin can pack _____ boxes. **Example 2** Divide. 1,200 ÷ 4 **STEP 1** Identify the basic fact. 12 ÷ 4 **STEP 2** Use place value. 1,200 = _____ hundreds 12 hundreds \div 4 = hundreds \leftarrow Think: 4 \times 3 hundreds = STEP 3 Divide. 12 hundreds =MATHEMATICAL PRACTICES $1,200 \div 4 = 300$ Math Talk Describe the pattern in the place value of the dividends and quotients. **Explain** how to use a basic fact and place value to divide $4,000 \div 5$.

WORLD

Share and Show

1. Divide. 2,800 ÷ 7

What basic fact can you use?

- 2,800 = 28
- 28 hundreds \div 7 =
- $2,800 \div 7 =$
- **2.** Divide. 280 ÷ 7

What basic fact can you use?

280 = 28

 $28 \text{ tens} \div = 4$

 $280 \div 7 =$

Use basic facts and place value to find the quotient.

| ∛ 3. 360 ÷ 6 = | 4. 2,000 ÷ 5 = | ∛ 5 . 4,500 ÷ 9 = |
|-----------------------|-----------------------|--------------------------|
|-----------------------|-----------------------|--------------------------|

On Your Own

Use basic facts and place value to find the quotient.

| 6. 560 ÷ 8 = | 7. 200 ÷ 5 = | 8. 240 ÷ 4 = |
|------------------------|------------------------|------------------------|
| 9. 810 ÷ 9 = | 10. 6,400 ÷ 8 = | 11. 3,500 ÷ 7 = |
| 12. 5,000 ÷ 5 = | 13. 9,000 ÷ 3 = | 14. 3,000 ÷ 5 = |

Algebra Find the unknown number.

15. $420 \div = 60$ **16.** $\div 4 = 30$ **17.** $810 \div = 90$

18. Explain how patterns and place value can help.

| | MATHEMATICAL PRACTICES |
|------------------|------------------------|
| Math Talk | Explain how |
| Exercises | 1 and 2 are alike |
| and diffe | erent. |

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| Name | | |
|---|---|--------------------------|
| | | |
| Find the quotient. 19. $25 \div 5 =$ | 20. 18 ÷ 2 = | 21. 63 ÷ 9 = |
| 250 ÷ 5 = | 180 ÷ 2 = | 630 ÷ 9 = |
| 2,500 ÷ 5 = | 1,800 ÷ 2 = | 6,300 ÷ 9 = |
| 22. Explain what you notice a | · · · · <u> </u> | |
| | | |
| | | |
| | | |
| Droblem Coluing | | |
| Problem Solving | WORLD | - SONT |
| 23. Jamal put 600 pennies int | | UNITED STAILS |
| pennies were in each roll? | | |
| | | |
| 24. Sela has 6 times as many 4 months ago. If Sela has 2 | | SHOW YOUR WORK |
| did she have 4 months ag | 0? | |
| | | |
| 25. The collected 2,09 | 90 dimes. Sue collected I all their dimes into 8 equal | |
| stacks. How many dimes a | | |
| | | |
| | | • |
| 26. Write Math > Mr. Rober | ts sees a rare 1937 penny. | |
| | 210. If he saves \$3 a week, igh money to buy the penny | |
| in one year? Explain. | ign money to buy the penny | • |
| | | |
| | | • |
| | | |
| | | • |
| | | Chapter 4 • Lesson 4 151 |

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- **27.** Carine sold \$320 worth of cookies. If each box of cookies costs \$4, how many boxes did she sell?
- 28. Test Prep Which number sentence is not true?
 - (A) $150 \div 5 = 30$ (C) $4,500 \div 9 = 500$
- **(B)** $400 \div 8 = 500$ **(D)** $5,600 \div 7 = 800$

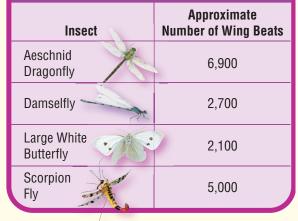
Connect to Science

Insect Flight

True flight is shared only by insects, bats, and birds. Flight in insects varies from the clumsy flight of some beetles to the acrobatic moves of dragonflies.

The wings of insects are not moved by muscles attached to the wings. Muscles in the middle part of the body, or thorax, move the wings. The thorax changes shape as the wings move.

Insect Wing Beats in 3 Minutes



- 29. About how many times does a damselfly's wings beat in 1 minute?
- **30.** About how many times do a scorpion fly's wings beat in 6 minutes?
- 31. Those minute, about how many more times do a damselfly's wings beat than a large white butterfly's wings?
- **32.** What's the Question? The answer is about 2,300 times.

Estimate Quotients Using

Compatible Numbers

Essential Question How can you use compatible numbers to estimate quotients?

UNLOCK the Problem TREAL

A horse's heart beats 132 times in 3 minutes. About how many times does it beat in 1 minute?

You can use compatible numbers to estimate quotients.

Compatible numbers are numbers that are easy to compute mentally.

Example 1 Estimate. 132 ÷ 3

STEP 1 Find a number close to 132 that divides easily by 3. Use basic facts.

 $12 \div 3$ is a basic fact. 120 divides easily by 3.

 $15 \div 3$ is a basic fact. 150 divides easily by 3.

Think: Choose 120 because it is closer to 132.

So, a horse's heart beats about _____ times a minute.

Example 2 Use compatible numbers to find two estimates that the quotient is between. $1,382 \div 5$

| STEP 1 Find two numbers close to 1,382 | STEP 2 Divide each number by 5. Use place value. | | | |
|--|---|--|--|--|
| that divide easily by 5. | 1,000 ÷ 5 | | | |
| ÷ 5 is a basic fact. 1,000 divides easily by 5. | hundreds ÷ 5 = hundreds, or | | | |
| ÷ 5 is a basic fact. 1,500 divides easily by 5. | 1,500 ÷ 5 | | | |
| 1,382 is between and | hundreds \div 5 = hundreds, or | | | |
| So, 1,382 ÷ 5 is between and | Explain which | | | |
| | estimate you think is more reasonable. | | | |

- Will a horse's heart beat more or fewer than 132 times in 1 minute?
- What operation will you use to solve the problem?

STEP 2 Use place value.

120 = tens

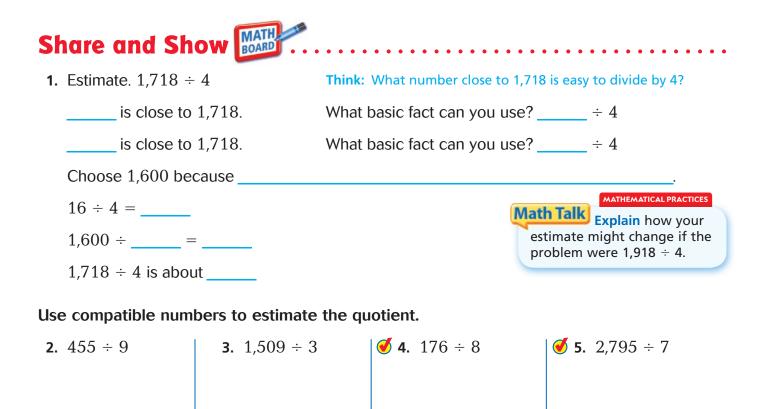
WORLD

12 ÷ 3 =

120 ÷ 3 =

 $12 \text{ tens} \div 3 = \text{tens}$

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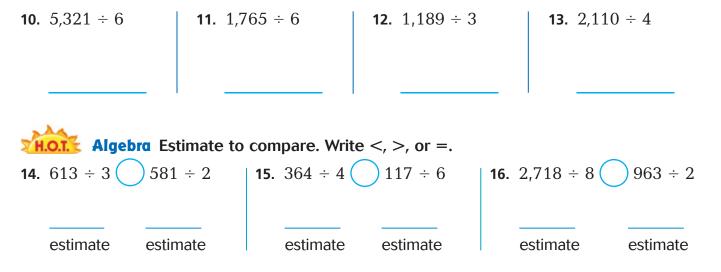


On Your Own

Use compatible numbers to estimate the quotient.

| 6. 163 ÷ 2 | 7. 500 ÷ 7 | 8. 1,421 ÷ 5 | 9. 2,642 ÷ 8 |
|-------------------|-------------------|---------------------|---------------------|
| | | | |
| | | | |
| | | | · |

Use compatible numbers to find two estimates that the quotient is between.



Problem Solving REAL WORLD

Use the table for 17–20.

- **17.** About how many times does a chicken's heart beat in 1 minute?
- **18.** About how many times does a cow's heart beat in 2 minutes?

Animal Heartbeats in 5 Minutes

| Animal | Number of Heartbeats | |
|---------|----------------------|------|
| Whale | 31 | |
| Cow | 325 | - |
| Pig | 430 | MA |
| Dog | 520 | 1 As |
| Chicken | 1,375 | - |

SHOW YOUR WORK

- **19.** About how many times faster does a cow's heart beat than a whale's?
- 20. Write Math >> What's the Question? The answer is about 100 beats in 1 minute.

- **21.** Jamie and his two brothers divided a package of 125 toy cars equally. About how many cars did each of them receive?
- 22. Test Prep A monkey's heart beats 1,152 times in 6 minutes. Which is the best estimate of the number of times its heart beats in 1 minute?

(A) 100

- **B** 200
- **(C)** 1,000
- **D** 2,000

Connect to Reading

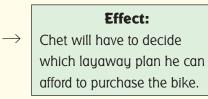
Cause and Effect

The reading skill cause and effect can help you understand how one detail in a problem is related to another detail.

Chet wants to buy a new bike that costs \$276. Chet mows his neighbor's lawn for \$15 each week. Since Chet does not have money saved, he needs to decide which layaway plan he can afford to buy the new bike.



Chet does not have money saved to purchase the bike.



Which plan should Chet choose?

| 3-month layaway: | 6-month layaway: |
|------------------|------------------|
| \$276 ÷ 3 | \$276 ÷ 6 |
| Estimate. | Estimate. |
| \$270 ÷ 3 | \$300 ÷ 6 |

Chet earns \$15 each week. Since there are usually 4 weeks in a month, multiply to see which payment he can afford.

\$15 × 4 = _____

So, Chet can afford the _____ layaway plan.

Use estimation to solve.

- **23.** Sofia wants to buy a new bike that costs \$214. Sofia helps her grandmother with chores each week for \$18. Estimate to find which layaway plan Sofia should choose and why.
- 24. Write Math Describe a situation when you have used cause and effect to help you solve a math problem.

Bike Shop Layaway Plans



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Division and the Distributive Property

Essential Question How can you use the Distributive Property to find quotients?

Investigate

Materials - color pencils - grid paper

You can use the Distributive Property to break apart numbers to make them easier to divide.

The Distributive Property of division says that dividing a sum by a number is the same as dividing each addend by the number and then adding the quotients.

A. Outline a rectangle on a grid to model $69 \div 3$.

Shade columns of 3 until you have 69 squares.

| | | | |
|------|------|------|------|------|------|------|------|------|------|--|------|--|
| | | | | | | | | | | | | |
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How many groups of 3 can you make?

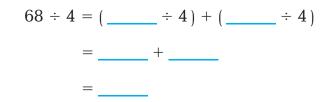
- **B.** Think of 69 as 60 + 9. Break apart the model into two rectangles to show $(60 + 9) \div 3$. Label and shade the smaller rectangles. Use two different colors.
- C. Each rectangle models a division.

$$69 \div 3 = (___ \div 3) + (___ \div 3)$$
$$= ___ + ___$$
$$=$$

D. Outline another model to show $68 \div 4$.

How many groups of 4 can you make?

E. Think of 68 as 40 + 28. Break apart the model, label, and shade to show two divisions.



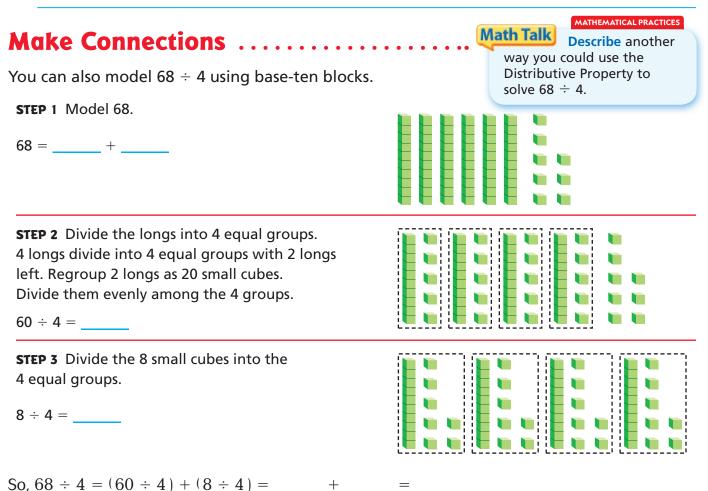
| 20 3 | 20 3 | | | | | | | | | | | | | + | + | + | + | + | - | H | | 1 | + | + | Ħ | Ħ | + | Ħ | 1 |
|-------|------|----|---|--|---|---|---|---|--------|---|-------|----|-----|---|-----|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| 2.0 3 | 3 | ## | + | | + | - | | | | - | | - | - | + | + | + | + | + | Ŧ | Ŧ | F | F | | 1 | + | P | 3 | 1 | - |
| | | | Ŧ | | + | E | | 2 | 0 | | | | | - | | - | + | + | + | + | 3 | + | | | + | | | | |
| | | ++ | 1 | | | - | 1 | | 1 | | 100 | 24 | 0 | | | | | | - | | T | T | 1 | F | | | - | | |
| | | 3 | | | | | | | STA BE | | 10445 | 12 | E E | | 200 | | | | | | 1 | 1 | 1 | ŧ | F | H | T | H | |



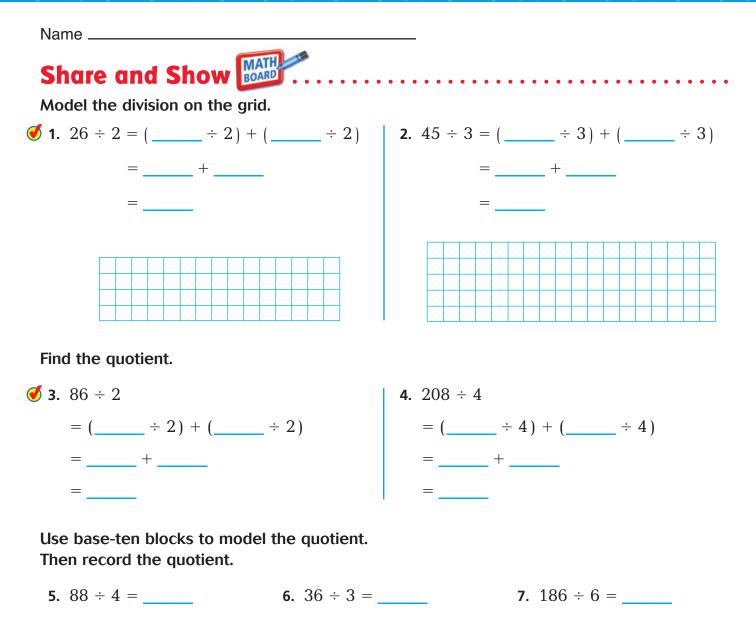
Draw Conclusions

1. Explain how each small rectangle models a quotient and a product in Step C.

- 2. Compare your answer in Step A to the final quotient in Step C. What can you conclude?
- **3. Evaluate** To find the quotient $91 \div 7$, would you break up the dividend into 90 + 1 or 70 + 21? Explain.



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9. 189 ÷ 9 =

12. 255 ÷ 5 =

- **8.** 96 ÷ 8 =
- **11.** 707 ÷ 7 =
- 14. **Write Math Explain** how you can model finding guotients using the Distributive Property.

10. 54 ÷ 2 =

13. 612 ÷ 6 =

Problem Solving REAL WORLD

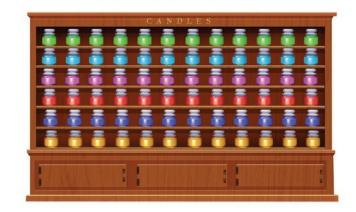
15. Christelle went to a gift shop. The shop sells candles in a variety of sizes and colors. The

Write a problem that can be solved using

picture shows a display of candles.

H.O.T. Pose a Problem

the picture.



| Pose a problem. | Solve your problem. |
|-----------------|---------------------|
| | |
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• **Describe** how you could change the problem by changing the number of rows of candles. Then solve the problem.



► Vocabulary

Choose the best term from the box to complete the sentence.

1. A number that is the product of a number and a counting

number is called a _____. (p. 137)

2. Numbers that are easy to compute mentally are called

_____. (p. 153)

3. When a number cannot be divided evenly, the amount

left over is called the _____. (p. 142)

Concepts and Skills

Divide. Draw a quick picture to help.

4. 26 ÷ 3 _____

5. 19 ÷ 4 _____

Use basic facts and place value to find the quotient.

6. $810 \div 9 =$ _____ **7.** $210 \div 7 =$ _____ **8.** $3,000 \div 6 =$ _____

Use compatible numbers to estimate the quotient.

 9. 635 ÷ 9
 10. 412 ÷ 5
 11. 490 ÷ 8

Use grid paper or base-ten blocks to model the quotient. Then record the quotient.

| 12. 63 ÷ 3 = | 13. 85 ÷ 5 = | 14. 168 ÷ 8 = |
|---------------------|---------------------|----------------------|
| | | |

- counting numbers
 - compatible numbers
 - multiple
 - remainder

Fill in the bubble completely to show your answer.

- **15**. Ana has 296 coins in her coin collection. She put the same number of coins in each of 7 jars. About how many coins are in each jar?
 - (A) about 20 coins
 - **B** about 40 coins
 - (C) about 200 coins
 - (D) about 400 coins
- **16**. Which two estimates is the quotient $345 \div 8$ between?
 - (A) 40 and 50 (C) 400 and 500
 - **B** 50 and 60 **D** 500 and 600
- 17. A peanut vendor had 640 bags of peanuts. She sold the same number of bags of peanuts at each of 8 baseball games. How many bags of peanuts did she sell at each game?

| A 8 | © 80 |
|-------------|----------------|
| B 10 | (D) 800 |

18. There are 4 students on a team for a relay race. How many teams can be made from 27 students?

| (A) 3 | © 6 |
|--------------|----------------|
| B 4 | (D) 7 |

19. Eight teams of high school students helped clean up trash in the community. Afterwards, they shared 23 pizzas equally. How many pizzas did each team get?

(B) $2\frac{3}{8}$ **(D)** 3

Name _____

Divide Using Repeated Subtraction

Essential Question How can you use repeated subtraction and multiples to find quotients?

Investigate

Materials counters grid paper

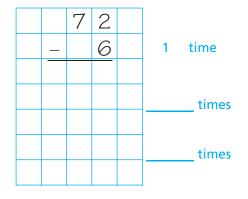
John is building a backyard pizza oven with an arch opening. He has 72 bricks. He will place 6 bricks at a time as he builds the oven. If he arranges the bricks in piles of 6, how many piles will he have?

You can use repeated subtraction to divide $72 \div 6$.

A. Begin with 72 counters. Subtract 6 counters.

How many are left?

B. Record the subtraction on grid paper as shown. Record the number of counters left and the number of times you subtracted.



D. Count the number of times you subtracted 6 counters.



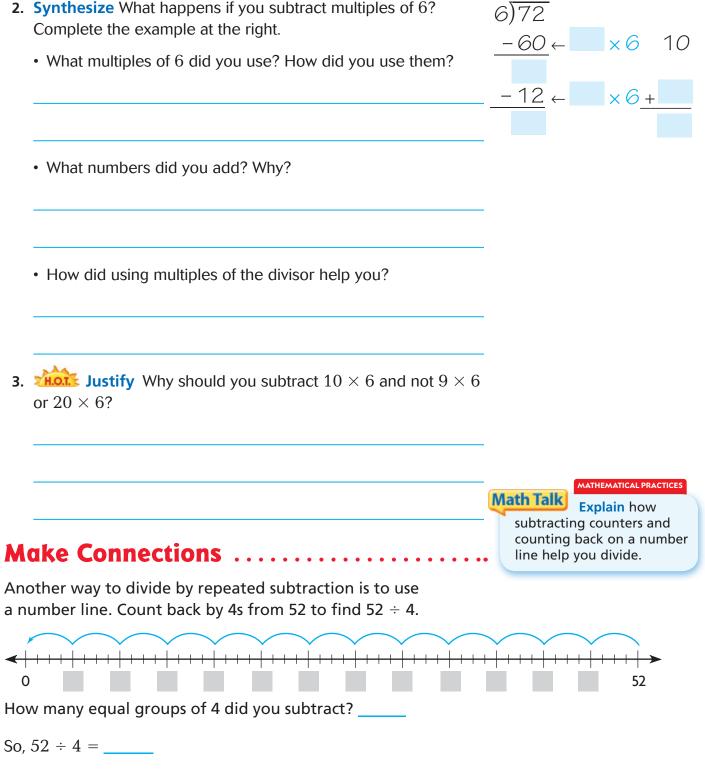
C. Can you reach zero evenly? Explain.

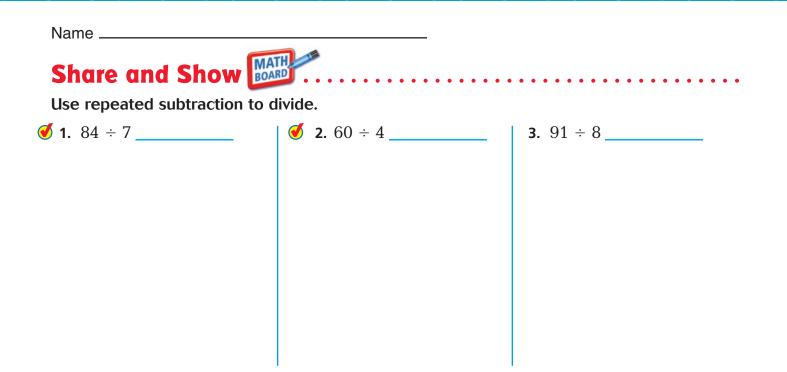
So, there are _____ piles of 6 bricks.

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Draw Conclusions

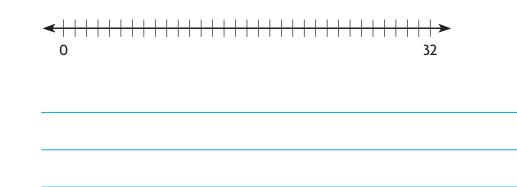
1. Explain the relationship between the divisor, the dividend, the quotient, and the number of times you subtracted the divisor from the dividend.





Draw a number line to divide.

- **4.** 65 ÷ 5 = _____
- **5.** 78 ÷ 6 = _____
- **6.** 91 ÷ 7 = _____
- 7. Write Math Can you divide 32 by 3 evenly? Use the number line to explain your answer.



| | | Mathematical Model • Reason • Make Sense | |
|----|--|--|--|
| | WNLOCK the Problem | WORLD | 7 |
| | A new playground will be 108 feet long. Buil allow 9 feet of space for each piece of climb They want to put as many climbers along the playground as possible. How many climbers What are you asked to find? | ilders need to bing equipment. he length of the | 1 |
| b. | How can you use repeated subtraction to so | olve the problem? | |
| C. | Tell why you might use multiples of the divise the problem. | sor to solve | |
| | | | |
| d. | Show steps to solve the problem. | e. Complete the sentences. There are equal parts of the playground, each feet long. So, climbers can fit along the length of the playground. | |
| 9. | There are 128 students in the fourth grade. Half of the students can use the playground at the same time. How many students is that? | 10. Test Prep An architect designed the school auditorium. There are 84 seats in Section A. Each row has 6 seats. How many rows of seats are in Section A? A 4 B 14 C 24 D 60 | Jgnon Millin Harcourt Fuulishing Company |
| | | | innu 🤊 |

Divide Using Partial Quotients

Essential Question How can you use partial quotients to divide by 1-digit divisors?

UNLOCK the Problem REAL WORLD

At camp, there are 5 players on each lacrosse team. If there are 125 people on lacrosse teams, how many teams are there?

One Way Use partial quotients.

In the **partial quotient** method of dividing, multiples of the divisor are subtracted from the dividend and then the partial quotients are added together.

Divide. 125 ÷ 5 Write. 5)125

STEP 1

Start by subtracting a greater multiple, such as 10 times the divisor. For example, you know that you can make at least 10 teams of 5 players.

Continue subtracting until the remaining number is less than the multiple, 50.

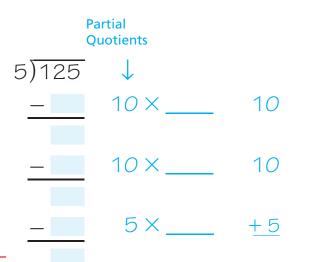
STEP 2

Subtract smaller multiples, such as 5, 2, or 1 times the divisor until the remaining number is less than the divisor. In other words, keep going until you no longer have enough players to make a team.

Then add the partial quotients to find the quotient.

So, there are lacrosse teams.

- Underline what you are asked to find.
- Circle what you need to use.
- What operation can you use to find the number of teams?

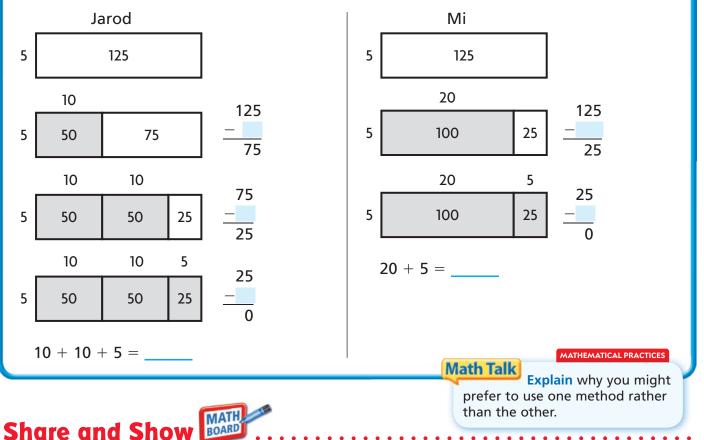


Math Talk

Explain how you found the total number of teams after finding the partial auotients.

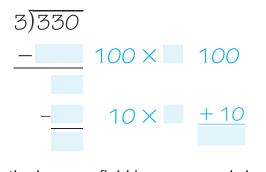
Another Way Use rectangular models to record the partial quotients.

Jarod and Mi also found the number of teams using partial quotients. They recorded the partial quotients using rectangular models. They each still had 25 as the quotient.



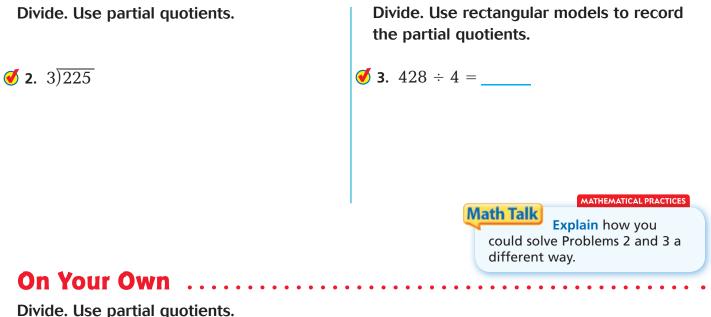
1. Lacrosse is played on a field 330 ft long. How many yards long is a lacrosse field? (3 feet = 1 yard)

Divide. Use partial quotients.



So, the lacrosse field is _____ yards long.

| Ν | а | m | ne | Э | |
|---|---|---|----|---|--|
| | | | | | |



Divide. Use partial quotients.

| 4. 9)198 | 5. 7) 259 | 6. 8) 864 | 7. 6)738 |
|-----------------|------------------|------------------|-----------------|
| | | | |
| | | | |
| | | | |
| | | | |

Divide. Use rectangular models to record the partial quotients.

 8. 328 ÷ 2 = ____
 9. 475 ÷ 5 = ____
 10. 219 ÷ 3 = ____
 11. 488 ÷ 4 = ____

Practice: Copy and Solve Divide. Use either way to record the partial quotients.

| 12. 875 ÷ 5 | 13. 372 ÷ 2 | 14. 252 ÷ 6 | 15. 429 ÷ 3 |
|--------------------|--------------------|--------------------|--------------------|
| 16. 568 ÷ 8 | 17. 504 ÷ 7 | 18. 624 ÷ 4 | 19. 819 ÷ 9 |

Problem Solving REAL WORLD

Model • Reason • Make Sense

Use the table for 20-22.

- 20. Rob wants to put 8 baseball cards on each page in an album. How many pages will he fill?
- **21.** Rob filled 9 plastic boxes with basketball cards with the same number of cards in each box. How many cards did he put in each box?



- 22. **Rot** Rob filled 3 fewer plastic boxes with football cards than basketball cards. How many boxes did he fill? How many football cards were in each box?
- 23. A professional game of lacrosse has 60 minutes of playing time. It is split into 4 equal periods of time. How many minutes are in each period?
- 24. Write Math What is the least number you can divide by 5 to get a three-digit quotient? Explain how you found your answer.

25. Test Prep There are 126 students who signed up to learn how to play lacrosse. If there are 6 students in each group, how many groups are there?

| A 12 | C 21 |
|-------------|--------------|
| B 20 | D 120 |



Model Division with Regrouping

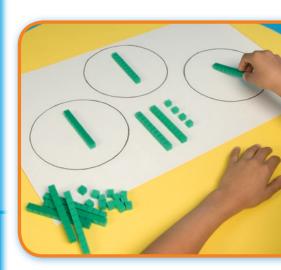
Essential Question How can you use base-ten blocks to model division with regrouping?

Investigate

Materials base-ten blocks

The librarian wants to share 54 books equally among 3 classes. How many books will she give to each class?

- **A.** Draw 3 circles to represent the classes. Then use base-ten blocks to model 54. Show 54 as 5 tens and 4 ones.
- **B.** Share the tens equally among the 3 groups.
- **C.** If there are any tens left, regroup them as ones. Share the ones equally among the 3 groups.
- **D.** There are _____ ten(s) and _____ one(s) in each group.
- So, the librarian will give _____ books to each class.



Draw Conclusions

- 1. **Explain** why you needed to regroup in Step C.
- **2.** Apply How you can use base-ten blocks to find the quotient of $92 \div 4$?

Make Connections

Use the quick picture at the bottom of the page to help you divide. Record each step.

. .

.

Find 76 ÷ 3.

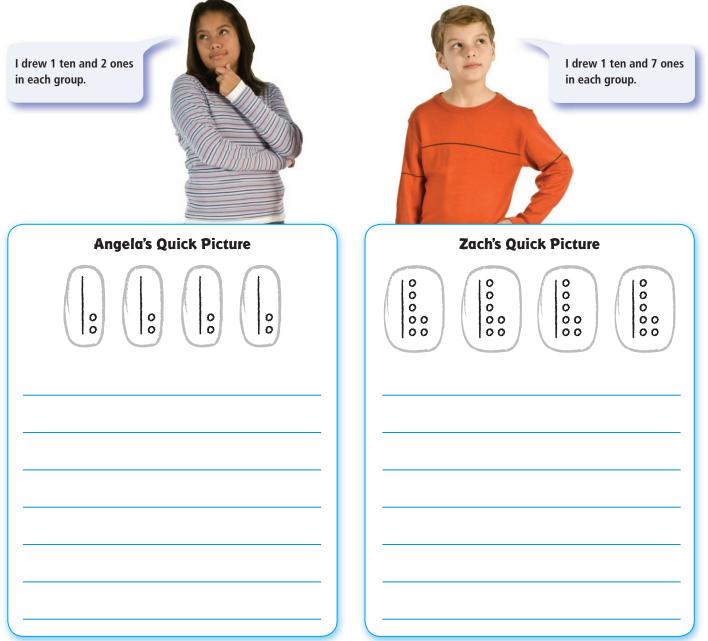
| STEP 1 Model 76 as 7 tens 6 ones. Draw three circles to represent equal groups. | 3)76 |
|--|--|
| STEP 2 Share the 7 tens equally among the 3 groups. Cross out the tens you use. | $\frac{1}{3}\overline{)76}$ tens in each group |
| There are tens in each group. | tens used |
| tens were used. There is ten left over. | ten left over |
| STEP 3 One ten cannot be shared among 3 groups without regrouping. Regroup 1 ten by drawing 10 ones. There are now ones to share. | $3)\overline{76}$ $-6 \checkmark$ ones to share |
| STEP 4 Share the ones equally among the 3 groups. Cross out the ones you use. | $3 \frac{2}{76}$ ones in each group |
| There are ones in each group. ones were used. There is one left over. | <u>-6</u> 16 _ ones used ✓ one left over |
| | |
| There are 3 groups of and left over. So, for $76 \div 3$, the quotient is and the remainder | Math Talk Why do you share tens equally among groups before sharing ones? |
| This can be written as | |

| I. 48 ÷ 3 | 2. 84 ÷ 4 | <i>ĕ</i> 3. 72 ÷ 5 |
|-----------------------|---------------------------|---|
| | | ∛ 3. 72 ÷ 5 |
| ivide. Draw quick pic | ctures. Record the steps. | |
| I. 59 ÷ 2 | | |
| | | —— tens in each group —— ones in each group |
| | <u></u> | |
| | 2)59 | <pre>tons used</pre> |
| | <u> </u> | tens used |
| | | ones to share |
| | | — one left over |
| 5. 84 ÷ 3 | | |
| | | tens in each group ones in each group |
| | | |
| | | |
| | 3)84 | ←— tens used |
| | 3)84 | tens used |
| | 3)84 | tens used ones to share ones used |
| | 3)84 | ones to share |
| | 3)84 | ones to share ones used |
| | 3)84 | ones to share ones used |

Problem Solving REAL WORLD

Sense or Nonsense?

Angela and Zach drew quick pictures to find 68 ÷ 4. Whose quick picture makes sense? Whose quick picture is nonsense?
 Explain your reasoning.

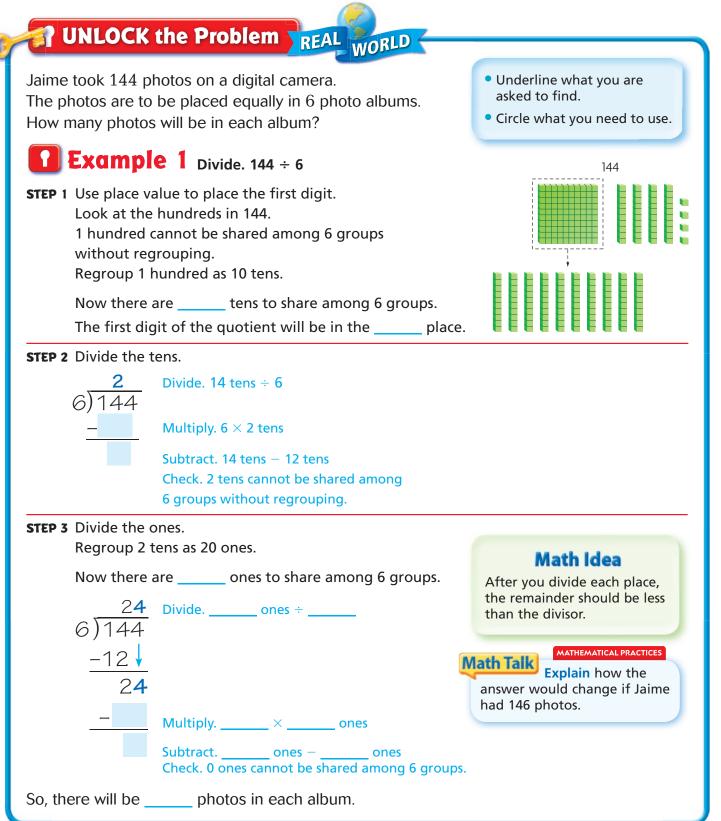


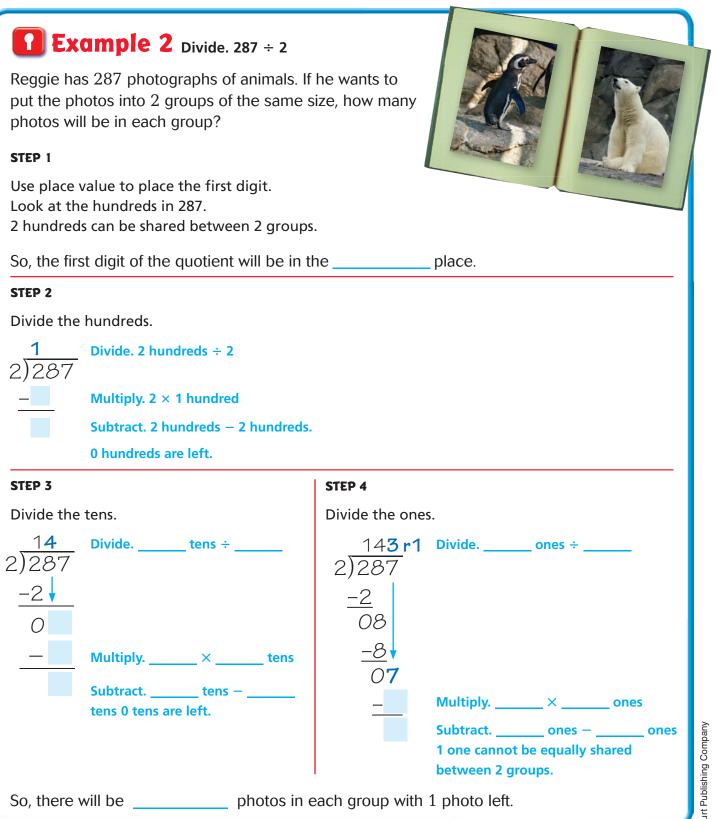
8. Analyze What did Angela forget to do after she shared the tens equally among the 4 groups?

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Place the First Digit

Essential Question How can you use place value to know where to place the first digit in the quotient?





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| How many pi | 2 pictures of dogs in 4 eq ctures are in each group? use place value to place t t. | Explain | 4)452 |
|--|---|-----------------------|---|
| | | | _ |
| ivide. | | | - |
| 2. 4) 166 | ∛ 3. 5)775 | 5 | |
|)n Your O | vn | Math Tal first dig | Explain how you placed the quotient in Exercise |
| 1. 4) 284 | 5 . 5) 394 | 6. 3)465 | 7. 8) 272 |
| | 9. 3) 504 | 10. 6)734 | 11. 4) 399 |
| 3. 2)988 | | | |
| | and Solve Divide. | | |
| 8. 2) 988 97actice: Copy 92. 516 ÷ 2 | and Solve Divide. 13. 516 ÷ 3 | 14. 516 ÷ 4 | 15. 516 ÷ 5 |

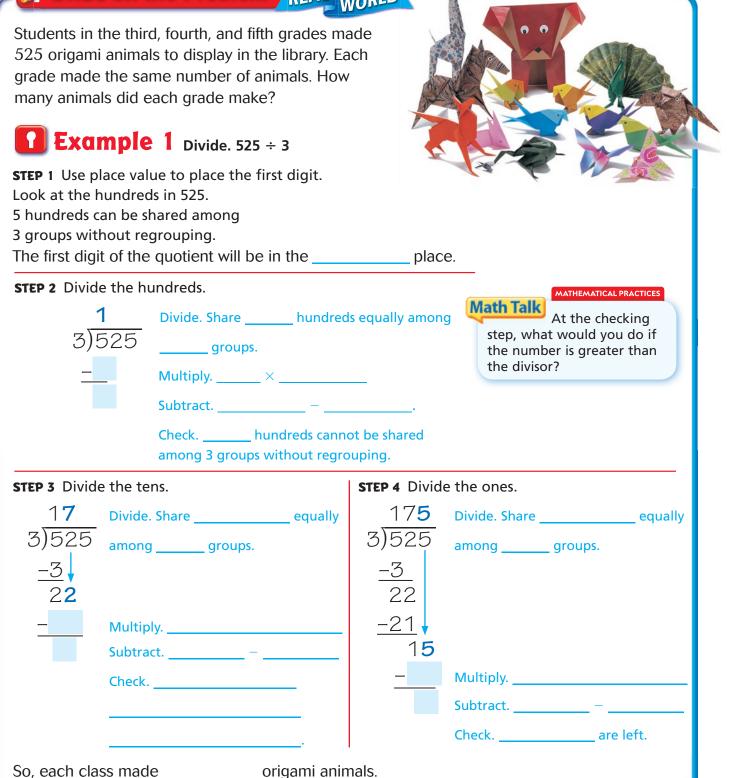
| | UNLOCK the Problem REAL | WONED | 655 | 90284 | |
|----|--|---|-------------------|---------------------------------------|--|
| | 17. Nan wants to put 234 pictures in an album with a blue cover. How many full pages will she have in her album? | | | | |
| a. | What do you need to find? | | Photo | Albums | |
| | | | Color of cover | Pictures per page | |
| b. | How will you use division to find the number | er of full pages? | Blue | 4 | |
| | | | Green | 6 | |
| | | | Red | 8 | |
| | Show the steps you will use to solve the problem. | She wants to with pages t She will have | pictures. | es in an album pictures. n full | |

- **18.** Juan wants to put his 672 pictures in an album with a green cover. How many full pages will he have in his album?
- **19. Test Prep** Kat wants to put her 485 pictures in an album with a red cover. She uses division to find out how many full pages she will have. In which place is the first digit of the quotient?
 - (A) thousands
 - (B) hundreds
 - C tens
 - **D** ones

Divide by 1-Digit Numbers

Essential Question How can you divide multidigit numbers and check your answers?

UNLOCK the Problem REAL WORLD



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There are 8,523 sheets of origami paper to be divided equally among 8 schools. How many sheets of origami paper will each school get?

Example 2 Divide. 8,523 ÷ 8

STEP 1 Use place value to place the first digit.

Look at the thousands in 8,523. 8 thousands can be shared among 8 groups without regrouping.

The first digit of the quotient will be

in the _____ place.

STEP 2 Divide the thousands.

STEP 3 Divide the hundreds.

STEP 4 Divide the tens.

STEP 5 Divide the ones.

So, each school will get _____ sheets of origami paper.

There will be _____ sheets left.

ERROR Alert

Place a zero in the quotient when a place in the dividend cannot be divided by the divisor.

CONNECT Division and multiplication are inverse operations. You can use multiplication to check your answer to a division problem.

Multiply the quotient by the divisor. If there is a remainder, add it to the product. The result should equal the dividend.

Divide.

| quotient | \rightarrow | 1,065 r3 | \leftarrow | remainder |
|----------|---------------|----------|--------------|-----------|
| divisor | \rightarrow | 8) 8,523 | \leftarrow | dividend |

| The share has a large state. | AL - A AL | | · |
|------------------------------|-----------|----------|-------------|
| The check shows | that the | division | is correct. |

Check.

8)8,523

| 1 | ,065 | \leftarrow | quotient |
|----------|------|--------------|-----------|
| \times | 8 | \leftarrow | divisor |
| 8 | ,520 | | |
| + | 3 | \leftarrow | remainder |
| 8 | ,523 | \leftarrow | dividend |

Name -

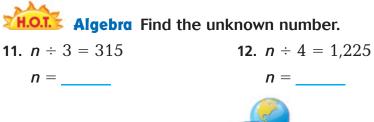
Share and Show

1. Ollie used 852 beads to make 4 bracelets. He put the same number of beads on each bracelet. How many beads does each bracelet have? Check your answer.



| Divide. | Check. | |
|---------------------------|-------------------|--|
| 2 4)852 | | MATHEMATICAL PRACTICES Math Talk Explain how you could check if your quotient |
| | | is correct. |
| So, each bracelet has bea | ids. | |
| Divide and check. | | |
| 2. 2)394 | 3. 2)803 | ∛ 4 . 4)3,448 |
| On Your Own | | |
| Divide and check. | ••••••• | • |
| 5. 2)816 | 6. 4)709 | 7. 3)267 |
| 8. 6)1,302 | 9. 8)9,232 | 10. 9)1,020 |

13. $185 = n \div 5$



Problem Solving REAL WORLD

Use the table for 14–16.

- 14. Four teachers bought 10 origami books and 100 packs of origami paper for their classrooms. They will share the cost of the items equally. How much should each teacher pay?
- 15. Write Math Six students shared equally the cost of 18 of one of the items in the chart. Each student paid \$24. What item did they buy? Explain how you found your answer.
- n =

 The Craft Store

 Item
 Price

 Origami Book
 \$24 each

 Origami Paper
 \$6 per pack

 Origami Kit
 \$8 each

SHOW YOUR WORK

- **16.** Ms. Alvarez has \$1,482 to spend on origami paper. How many packs can she buy?
- 17. Evan made origami cranes with red, blue, and yellow paper. The number of cranes in each color is the same. If there are 342 cranes, how many of them are blue or yellow?
- 18. Test Prep An artist made 515 origami animals in 5 days. She made the same number of animals each day. How many origami animals did she make each day?

| A | 13 | | C | 510 |
|---|----|--|---|-----|
|---|----|--|---|-----|

B 103 **D** 2,060

Problem Solving • Multistep Division Problems

Essential Question How can you use the strategy *draw a diagram* to solve multistep division problems?

WILOCK the Problem

Lucia and her dad will prepare corn for a community picnic. There are 3 bags of corn. Each bag holds 32 ears of corn. When the corn is cooked, they want to divide the corn equally among 8 serving plates. How many ears of corn should they put on each of 8 serving plates?



Read the Problem

What do I need to find?

I need to find the number of _____ that

will go on each plate.

What information do I need to use?

_ bags with _____ ears in each bag.

The total ears are divided equally into _____

groups.

How will I use the information?

I will make a bar model for each step

to visualize the information. Then I will

to find the total and _____

to find the number for each plate.

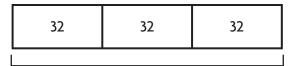


2. How can you check your answer?_____

Solve the Problem

I can draw bar models to visualize the information given and then decide how to find how many ears of corn should go on a plate.

First, I will model and multiply to find the total number of ears of corn.



Then I will model and divide to find how many ears of corn should go on each plate.



1 Try Another Problem

There are 8 dinner rolls in a package. How many packages will be needed to feed 64 people if each person has 2 dinner rolls?



| Read the Problem | Solve the Problem |
|---|-------------------|
| What do I need to find? | |
| What information do I need to use? | |
| How will I use the information? | |
| 3. How many packages of rolls will be needed? _4. How did drawing a bar model help you solve t | Describe another |
| | |

Name

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Share and Show

 A firehouse pantry has 52 cans of vegetables and 74 cans of soup. Each shelf holds 9 cans. What is the least number of shelves needed for all the cans?

First, draw a bar model for the total number of cans.

Next, add to find the total number of cans.

UNLOCK the Problem

Use the Problem Solving MathBoard.

- Underline important facts.
- Choose a strategy you know.

Math Talk Explain how you could check that your answer is correct.

SHOW YOUR WORK

Then, draw a bar model to show the number of shelves needed.

Finally, divide to find the number of shelves needed.

So, ______ shelves are needed to hold all of the cans.

 What if 18 cans fit on a shelf? What is the least number of shelves needed? Describe how your answer would be different.

Julio's dad bought 10 dozen potatoes. The potatoes were equally divided into 6 bags. How many potatoes are in each bag?

 Ms. Johnson is in charge of decorations for a party. She bought 6 bags of balloons. Each bag has 25 balloons. She fills all the balloons and puts 5 balloons in each bunch. How many bunches can she make?

THEMATICAL Model • Reason • Make Sense

On Your Own

- 5. At the garden shop, each small tree costs \$125 and each large tree costs \$225. How much will 3 small trees and 1 large tree cost?
- An adult's dinner costs \$8. A family of 2 adults and 2 children pays \$26 for their dinners. How much does a child's dinner cost? Explain.

Choose a STRATEGY

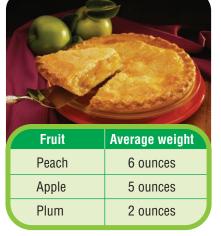
Act It Out Draw a Diagram Find a Pattern Make a Table or List Solve a Simpler Problem

Use the table for 7–8.

Write Math Maria bought 80 ounces of apples. She needs 10 apples to make a pie. How many apples will be left over? Explain.

- 8. Molly put 4 pieces of fruit in a bag. The bag weighs 19 ounces. How many of each kind of fruit are in the bag?
 - 9. The garden warehouse delivered 1,500 pounds of topsoil in 5-pound bags to the garden shop. The garden shop sold half of the bags the same day they were delivered. How many bags does the garden shop have left to sell?
 - Test Prep Ben collected 43 cans and some bottles. He received 5¢ for each can or bottle. If Ben received a total of \$4.95, how many bottles did he collect?

(A) 56 **(B)** 99 **(C)** 560 **(D)** 990



Name .



Vocabulary

Choose the best term from the box.

1. When a number cannot be divided evenly, the amount

left over is called the _____. (p. 142)

2. You use the _____ method of dividing when multiples of the divisor are subtracted from the dividend and then the quotients are added together. (p. 167)

Vocabulary

compatible numbers

partial quotient

remainder

Concepts and Skills

Use grid paper or base-ten blocks to model the quotient. Then record the quotient.

| 3. 96 ÷ 6 = | 4. 86 ÷ 2 = | 5. 155 ÷ 5 = |
|--------------------|--------------------|---------------------|
| | | |

Find two numbers the quotient is between. Then estimate the quotient.

| 6. 787 ÷ 2 | 7. 391 ÷ 6 | 8. 789 ÷ 8 |
|-------------------|-------------------|-------------------|
| | | |
| | | |
| District | | 1 |

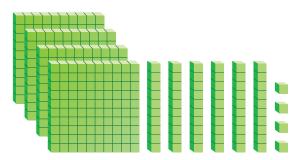
Divide.

 9. $3\overline{)987}$ 10. $7\overline{)501}$ 11. $5\overline{)153}$

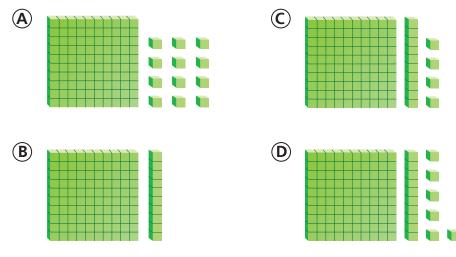
 12. $4\overline{)808}$ 13. $6\overline{)8,348}$ 14. $8\overline{)4,897}$

Fill in the bubble completely to show your answer.

- **15.** There are 96 tourists who have signed up to tour the island. The tourists are assigned to 6 equal-size groups. How many tourists are in each group?
 - **A** 1 r3
 - **B** 1 r6
 - **(C)** 11
 - **D** 16
- **16.** Maria needs to share the base-ten blocks equally among 4 equal groups.



Which model shows how many are in each equal group?

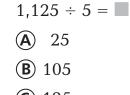


- **17.** Manny has 39 rocks. He wants to put the same number of rocks in each of 7 boxes. Which sentence shows how many rocks will be in each box?
 - A He will need 6 boxes.
 - **B** There will be 6 rocks in each box.
 - C There will be 5 rocks in each box.
 - **D** There will be 5 rocks left over.

Name .

Fill in the bubble completely to show your answer.

- **18.** There are 176 students in the marching band. They are arranged in equal rows of 8 students for a parade. How many rows of students are there?
 - (A) 220 rows
 - **B** 120 rows
 - C 22 rows
 - **D** 21 rows
- **19.** Naomi wants to plant 387 tulip bulbs in 9 equal rows. She uses division to find the number of tulips in each row. In which place is the first digit of the quotient?
 - (A) ones
 - **B** tens
 - C hundreds
 - **D** thousands
- **20.** Kevin and 2 friends are playing a game of cards. There are 52 cards in the deck to be shared equally. Kevin wants each player to receive the same number of cards. How many cards will each player receive? How many cards will be left over?
 - (A) 16 cards and 4 cards left over
 - (B) 17 cards and 1 card left over
 - C 25 cards and 2 cards left over
 - (D) 26 cards and no cards left over
- 21. Which number is the quotient?



- **(C)** 125
- **D** 225

Constructed Response

22. Mrs. Valdez bought 6 boxes of roses. Each box had 24 roses. She divided all the roses into 9 equal bunches. How many roses were in each bunch? Explain how to use a diagram to help solve the problem. Show your diagrams.

Performance Task

23. Mr. Owens plans to rent tables for a spaghetti fundraiser. He needs to seat 184 people.



A If Mr. Owens wants all rectangular tables, how many tables should he rent? **Explain.**

B Square tables rent for \$12 each. Circular tables rent for \$23 each. Mr. Owens says it would cost him less to rent square tables instead of circular tables. Is he right? Explain.